A Flexible Simulation Tool for Estimating Data Loss Risks in Storage Arrays

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Abstract—Proteus is an open-source simulation program that can predict the risk of data loss in many disk array configurations, among which, mirrored disks, all levels of RAID arrays and various two-dimensional RAID arrays. It characterizes each array by five numbers, namely, the size $n$ of the array, the number $n_f$ of simultaneous disk failures the array will always tolerate without data loss, and the respective fractions $f_1$, $f_2$ and $f_3$ of simultaneous failures of $n_f+1$, $n_f+2$ and $n_f+3$ disks that will not result in a data loss. As with any simulation tool, Proteus imposes no restriction on the distributions of failure and repair events. Our measurements have shown a surprisingly good agreement with the results obtained through analytical techniques and no measurable difference between values obtained assuming deterministic repair times and those assuming exponential repair times.

I. INTRODUCTION

Providing trustworthy estimates of the reliability of fault-tolerant disk arrays is a difficult task because analytical techniques are based on assumptions that are never realized in practice and simulation techniques require writing a new simulation program for each array organization we want to investigate.

We wrote the Proteus simulation program to address these issues. First, Proteus is flexible and can be parameterized to model most fault-tolerant disk array organizations. Second, Proteus is designed to run fast, which is important because obtaining tight confidence intervals for the reliability of highly fault-tolerant disk arrays often requires millions of simulation runs. Finally, Proteus is written in Python 3, a freely available language that has been ported to many programming environments.

We used Proteus to evaluate the five-year reliability of various fault-tolerant disk array organizations, including RAID levels 4, 5, and 6 and two-dimensional RAID arrays. Our results show excellent agreement with the five-year reliability figures obtained through analytical techniques. In addition, they presented no difference between the values obtained assuming deterministic repair times and those assuming exponential repair times.

II. FAULT- TOLERANT DISK ARRAYS

RAID arrays were the first disk array organizations to utilize erasure coding in order to protect data against disk failures [15, 20, 4]. While RAID levels 3, 4 and 5 only tolerate single disk failures, RAID level 6 organizations use $(n-2)$-out-of-$n$ codes to protect data against double disk failures [2]. EvenOdd, Row-Diagonal Parity and the Liberation Codes are three implementations of RAID level 6 that use only XOR operations to construct their parity information [1, 6, 7, 17]. Corbett et al. then Huang and Xu as well as Goel and Corbett proposed coding schemes correcting triple failures [5, 10, 8].

Two popular combinations of RAID organizations are RAID 10 and RAID 01. RAID 10 organizations group their constituent disks into pairs of mirrored disks and combines these pairs of disks into a RAID level 0 organization. Conversely, RAID 01 organizations consist of two RAID level 0 arrays that mirror each other.

Two-dimensional RAID arrays, or 2D-Parity arrays, such as the one displayed in Fig. 1, were investigated by Schwarz [19] and Hellerstein et al. [9]. Hellerstein noted that these arrays tolerate all double disk failures while Schwarz observed that they also tolerate most triple or quadruple disk failures. More recently, Lee patented a two-dimensional disk array organization implementing prompt parity updates in one dimension and delayed parity updates in the second dimension.
[12]. Pâris et al. [13] investigated two-dimensional RAID arrays that could reorganize themselves after a disk failure.

III. THE PROTEUS SIMULATOR

Our main motivation for using a simulation approach was its higher accuracy. While Markov models require disk failure and repair processes to obey a Poisson law, simulation allows us to use arbitrary distributions, including failure distributions describing variable failure rates and repair time distributions with smaller coefficients of variation than the exponential distribution.

At the same time, we wanted to avoid the two main disadvantages of the simulation approach, namely the need to write a different simulation program for each array configuration being investigated and the long simulation runs. This latter consideration was especially important in our case because data losses are rare events and we might have to perform hundreds of thousands or even millions of runs of our model in order to observe a single data loss.

In other words, we wanted to develop a simulation program that was both very flexible and very fast. These two objectives were met by using a very simple and very flexible disk array model, which we will describe next.

A. The disk array model

A key feature of Proteus is its disk array model: it describes the topology of any disk array using only five parameters, namely:

1. The total number of disks \( n \) in the array;
2. The number \( n_f \) of simultaneous disk failures the array will always tolerate without data loss;
3. The fraction \( f_1 \) of simultaneous failures of \( n_f + 1 \) disks that will not result in a data loss;
4. The fraction \( f_2 \) of simultaneous failures of \( n_f + 2 \) disks that will not result in a data loss;
5. The fraction \( f_3 \) of simultaneous failures of \( n_f + 3 \) disks that will not result in a data loss.

For instance, we can characterize all RAID level 1 to 5 by their size and the four parameters

\[ n_f = 1, f_1 = f_3 = 0, \]

because these organizations tolerate all single disk failures and no double disk failures. The case of RAID level 6 arrays is fairly similar: they can be characterized by their sizes and the four parameters

\[ n_f = 2, f_1 = f_2 = f_3 = 0. \]

For more complex disk array configurations, we cannot assume that the three parameters \( f_1, f_2, \) and \( f_3 \) are equal to zero because doing so would underestimate the array reliability. Consider for instance the two-dimensional disk array depicted in Fig. 1. As we can see in Fig. 2, the failure of an arbitrary data disk (\( D_{22} \) in our example) and its two parity disks (\( P_2 \) and \( Q_2 \)) will always result in a data loss. We observe that these triple failures represent only a small fraction of all potential triple disk failures: for a two-dimensional disk array with \( n^2 \) data disks and \( 2n \) parity disks, only \( n^2 \) out of the \( \binom{n^2 + 2n}{3} \) possible triple failures are fatal. As the size of the array grows, the ratio

\[ \alpha = \frac{n^2}{\binom{n^2 + 2n}{3}} \]

quickly decreases: it becomes less than 1 percent for \( n \geq 4 \) and less than 0.1 percent for \( n \geq 8 \). Conversely, the fraction \( f_1 = 1 - \alpha \) of triple failures the array will tolerate without data loss goes closer to unity as the size of the array increases.

Let us now consider quadruple failures. As Fig. 3 shows, the sole quadruple disk failures resulting in a data loss are:

1. The failure of a data disk, its two parity disks and any other disk; and
2. The failure of four disks placed at the summits of a rectangle.

Out of the \( \binom{n^2 + 2n}{4} \) possible quadruple failures the array can experience, we can enumerate:

1. \( n^2(n^2 + 2n - 3) \) failures of a data disk, its two parity disk and any of the \( n^2 + 2n - 3 \) remaining disks;
2. \( \binom{n^2}{2} + 2n \binom{n}{2} \) failures of four disks placed at the summits of a rectangle;

for a total of \( n^2(n^2 + 2n - 3) + \binom{n^2}{2} + 2n \binom{n}{2} \) fatal quadruple failures.

As we observed for triple failures, the fraction

\[ \beta = \frac{n^2(n^2 + 2n - 3) + \binom{n^2}{2} + 2n \binom{n}{2}}{\binom{n^2 + 2n}{4}} \]
of fatal quadruple failures decreases with the size of the array: it becomes less than 4 percent for \( n \geq 4 \) and less than 0.4 percent for \( n \geq 8 \). In the same way, the fraction \( f_2 = 1 - \beta \) of quadruple failures that the array will tolerate without data loss goes closer to unity as the size of the array increases.

We could, if we wanted, extend this approach to quintuple failures or even sextuple failures. We should however keep in mind that disk repair rates typically are more than one thousand times faster than their failure rates. As a result, each individual disk is likely to remain operational most of the time and the probability that any reasonably-sized disk array will experience five or six simultaneous disk failures is very low. Hence, we can safely assume that \( f_3 = 0 \). We nevertheless decided to keep this parameter as it might be useful for simulating very large disk arrays. The other parameters of our model are the disk failure and repair time distributions.

In addition to its flexibility, our disk array model results in a very simple simulation model: it represents the disk array being investigated as a single entity whose state is described by its number of failed disks. This number will be decreased by one each time a failure event occurs and increased by one each time a disk gets repaired.

At the same time our model has four important limitations. First, it assumes that all disks have the same failure and repair distributions. The main reason for this restriction was keeping the simulator simple by limiting the number of its input parameters.

Second, our model assumes that disk failures and repair are independent events. The main reasons for our choice were keeping the simulator simple and the lack of a community consensus on how to model correlated failures.

Third, our model imposes some restrictions on the disk repair process. It postulates that there will be no delay between the time a disk failure occurs and the start of the repair process. In addition, it also assumes that disk repairs can proceed in parallel without interfering with each other.

Fourth, our model assumes that we can safely neglect the probability that the disk array will experience more than \( n_f + 3 \) simultaneous disk failures and still undergo no data loss. This assumption is strictly true for RAID organizations 0 to 6 as they always experience a data loss after the simultaneous failure of more than \( n_f \) disks. It is fairly accurate for more complex disk array organizations as long they do not exceed, say, a few hundred disks.

### B. Selecting a reliability index

Most extant studies of disk array reliability use array mean time to data loss (MTTDL) as reliability index because it can be easily computed through analytical methods. We decided in favor of a more realistic index of disk array reliability, namely, their five-year reliability. It represents the probability that a given array will not experience a data loss over a useful lifetime of five years. In addition to being a better index of actual disk array reliability, five-year reliabilities can be directly measured through simulation by repeatedly simulating the behavior of a disk array over a period of five years and counting the number of times a data loss occurred.

### C. Simulation support

Given the simplicity of our model, we decided to use a general-purpose programming language and selected Python for three reasons. First, it is freely available on many computing platforms, among which Windows, Linux/Unix, Mac OS X, as well as the Java and .NET virtual machines. Second, its extensive libraries include good random number generators for the exponential and Weibull distribution as well as a fast built-in implementation of heaps. Finally, the conciseness of the language results in a more readable program.

### D. Proteus organization

Proteus consists of an input phase, a simulation phase and a very short data analysis phase. The input phase prompts users for the parameters of the system in a self-explanatory fashion. The current implementation of Proteus offers two choices for the failure time distribution, namely, exponential and Weibull, as well as two possible repair time distributions, namely, exponential and deterministic. While the exponential distribution remains the “safe” traditional choice for modeling disk failures, the Weibull distribution allows users to study the behavior of disk arrays subject to either infant disk mortality during their early months or increased failure rates as the array ages. In the same way, deterministic repair times are a good proxy for all repair time distributions with a smaller coefficient of variation than the exponential distribution.

The simulation phase consists of repeated runs of the simulation model. The main issue here is that we are simulating disk arrays that are not likely to fail during their useful lifetime. In some cases, we may thus have to simulate hundreds or thousands of runs in order to observe one data loss.
Finally, the data analysis phase computes a confidence interval for the five-year reliability of the array. As these values are fairly close to 1, we express them in “nines” using the formula
\[ n_d = \log_{10}(1 - R_d) \], where \( R_d \) is the five-year reliability of the array. Thus a reliability of 0.999 would be represented by 3 nines, a reliability of 0.9999 by 4 nines and so on.

IV. Experimental Results

We present two series of experimental results comparing the reliability figures obtained by Proteus with those derived from analytical models. Since the outcomes of these analytical models were mean times to data loss (MTTDLs), these values were converted into five-year reliabilities using the formula
\[ R_d = \exp\left(-\frac{d}{MTTDL}\right) \]
where \( d \) is a five-year interval expressed in the same units as the MTTDL. Observe that the above formula implicitly assumes that the array long-term failure rate \( 1/MTTDL \) does not significantly differ from the average failure rate during the first five years of the array.

A. Evaluating the impact of repair times distributions on the reliability of RAID arrays level 5 and 6

In our first series of experiments, we measured the five year reliabilities of two distinct RAID arrays assuming both exponential and deterministic repair times and compared these values with those obtained through analytical techniques.

The first array we investigated was a RAID level 5 array consisting of five disks with parity data that occupy 20 percent of the disk space. The second disk array was a RAID level 6 array with 10 disks with the same space overhead as the first array.

We assumed a disk mean time to fail (MTTF) of one hundred thousand hours, which corresponds to slightly less than one failure every eleven years. This rate is at the high end of the failure rates observed by Pinheiro et al. [16] as well as Schroeder and Gibson [18]. The three disk mean times to repair (MTTRs) we selected were one day, two days and five days. All simulations were repeated three times.

Since RAID level 5 arrays tolerate at most one disk failure while RAID level 6 arrays tolerate at most two disk failures, the topology of our RAID level 5 array was modeled with the five parameters
\[ n_f = 5, n_f = 1, f_1 = f_2 = f_3 = 0, \]
and that of our level 6 array with the parameters
\[ n_f = 10, n_f = 2, f_1 = f_2 = f_3 = 0. \]

Tables I to IV summarize our results. As we can see, the five-year reliability values obtained through stochastic methods always fall inside our confidence intervals. In addition, we did not observe any significant difference between the reliability figures for deterministic repair times and those for exponential repair times. This confirms earlier observations made by Carroll and Long on the impact of repair time distributions on the availability of replicated data in the presence of site failures [3].

### Table I. Confidence intervals for the five-year reliability of a RAID level 5 array with five disks assuming deterministic repair times.

<table>
<thead>
<tr>
<th>Disk MTTF: 100,000 hours</th>
<th>MTTR</th>
<th>One Day</th>
<th>Two Days</th>
<th>Five Days</th>
</tr>
</thead>
<tbody>
<tr>
<td>Array Reliability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Run 1</td>
<td>2.67</td>
<td>2.68</td>
<td>2.37</td>
<td>2.38</td>
</tr>
<tr>
<td>Run 2</td>
<td>2.67</td>
<td>2.68</td>
<td>2.37</td>
<td>2.38</td>
</tr>
<tr>
<td>Run 3</td>
<td>2.67</td>
<td>2.68</td>
<td>2.37</td>
<td>2.38</td>
</tr>
</tbody>
</table>

### Table II. Confidence intervals for the five-year reliability of a RAID level 5 array with five disks assuming exponential repair times.

<table>
<thead>
<tr>
<th>Disk MTTF: 100,000 hours</th>
<th>MTTR</th>
<th>One Day</th>
<th>Two Days</th>
<th>Five Days</th>
</tr>
</thead>
<tbody>
<tr>
<td>Array Reliability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Run 1</td>
<td>4.94</td>
<td>5.12</td>
<td>4.42</td>
<td>4.52</td>
</tr>
<tr>
<td>Run 2</td>
<td>4.94</td>
<td>5.12</td>
<td>4.44</td>
<td>4.53</td>
</tr>
<tr>
<td>Run 3</td>
<td>4.97</td>
<td>5.16</td>
<td>4.39</td>
<td>4.47</td>
</tr>
</tbody>
</table>

### Table III. Confidence intervals for the five-year reliability of a RAID level 6 array with ten disks assuming deterministic repair times.

<table>
<thead>
<tr>
<th>Disk MTTF: 100,000 hours</th>
<th>MTTR</th>
<th>One Day</th>
<th>Two Days</th>
<th>Five Days</th>
</tr>
</thead>
<tbody>
<tr>
<td>Array Reliability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Run 1</td>
<td>4.94</td>
<td>5.12</td>
<td>4.42</td>
<td>4.52</td>
</tr>
<tr>
<td>Run 2</td>
<td>4.94</td>
<td>5.12</td>
<td>4.44</td>
<td>4.53</td>
</tr>
<tr>
<td>Run 3</td>
<td>4.97</td>
<td>5.16</td>
<td>4.39</td>
<td>4.47</td>
</tr>
</tbody>
</table>

### Table IV. Confidence intervals for the five-year reliability of a RAID level 6 array with ten disks assuming exponential repair times.

<table>
<thead>
<tr>
<th>Disk MTTF: 100,000 hours</th>
<th>MTTR</th>
<th>One Day</th>
<th>Two Days</th>
<th>Five Days</th>
</tr>
</thead>
<tbody>
<tr>
<td>Array Reliability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Run 1</td>
<td>5.04</td>
<td>5.16</td>
<td>4.43</td>
<td>4.47</td>
</tr>
</tbody>
</table>

B. Two-dimensional RAID arrays

We present here results for a two-dimensional RAID array model with 64 data disks plus 16 parity disks and no superparity disk. Like the two RAID organizations we previously investigated the space overhead of this array is 20 percent. Space considerations prevent us from discussing here the case of two-dimensional arrays with a superparity disk. Interested readers are referred to Kao’s thesis [11].

Because the array tolerates all double disk failures without a data loss but not all triple failures, its \( n_f \) parameter is set to two. As we did in Section 2, we assume that the array will tolerate most triple and quadruple failures but neglect to take
into account the probability of no data loss after a quintuple failure. As a result, the values of its $f_1, f_2$ and $f_3$ parameters are

$$f_1 = 1 - \alpha = 0.999221, f_2 = 1 - \beta = 0.996105, f_3 = 0$$

As before, the disk MTTF was set to 100,000 hours. We assumed exponential repair times and this time investigated a range of disk repair times extending from half a day to ten days. The results of our simulations were compared to the results obtained through Markov analysis and presented in a previous paper [14].

As Table V shows, almost all five-year reliability values obtained through stochastic methods fall inside our confidence intervals. In addition, we observe that our two-dimensional RAID organization offers better five-year reliability figures than the RAID level 6 array with eight data disks and two parity disks that we have just discussed. This is a superb result when we consider that our two-dimensional array has the same space overhead as the RAID level 6 array and holds eight times as much data.

V. CONCLUSION

Previously, practitioners who desired to obtain good estimates of the reliability of a disk array were forced to choose between accepting the limits of analytical methods and having to write a different simulation program for each disk array configuration.

We have presented Proteus, a flexible portable simulation tool for evaluating the risk of data loss in fault-tolerant disk arrays. Its main advantage is its ability to simulate a wide range of disk array configurations without any reprogramming. This was made possible through the key observation that disk array reliability can be characterized by the probability that the array will survive a given number of disk failures.

Proteus is an open-source program that will be made available from the web site of the Storage Systems Research Center of the University of California, Santa Cruz (www.ssrc.ucsc.edu) and the personal web site of one of the authors (www.cs.uh.edu/~paris/Proteus).

### REFERENCES


### Table V. Confidence intervals for the five year reliability of a two-dimensional RAID array with 64 data disks and 16 parity disks.

<table>
<thead>
<tr>
<th>MTTR (days)</th>
<th>L-bound (nines)</th>
<th>U-bound (nines)</th>
<th>Analytic (nines)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>5.739</td>
<td>6.863</td>
<td>5.911</td>
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<tr>
<td>1</td>
<td>5.079</td>
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<td>5.295</td>
</tr>
<tr>
<td>1.5</td>
<td>4.783</td>
<td>5.023</td>
<td>4.923</td>
</tr>
<tr>
<td>2</td>
<td>4.505</td>
<td>4.673</td>
<td>4.649</td>
</tr>
<tr>
<td>2.5</td>
<td>4.365</td>
<td>4.505</td>
<td>4.426</td>
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<td>3</td>
<td>4.206</td>
<td>4.321</td>
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<td>3.5</td>
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<td>4.100</td>
<td>4.068</td>
</tr>
<tr>
<td>4</td>
<td>3.911</td>
<td>3.991</td>
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<tr>
<td>4.5</td>
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<td>5</td>
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</tr>
<tr>
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<td>3.444</td>
<td>3.421</td>
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<td>6.5</td>
<td>3.295</td>
<td>3.333</td>
<td>3.317</td>
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